# Thermodynamic Properties of Ternary Mixtures. 2. The Excess Volumes of Mixing of Ternary Mixtures of Cyclohexane, Aromatics, and Halomethanes 

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The excess volumes of mixing of seven ternary mixtures, viz., (i) carbon tetrachloride $\left(\mathrm{CCl}_{4}\right)+$ benzene $+p$-xylene, (ii) cyclohexane $+\mathrm{CCl}_{4}+$ toluene, (iii) cyclohexane + $\mathrm{CCl}_{4}+p$-xylene, (iv) cyclohexane + chloroform ( $\mathrm{CHCl}_{3}$ ) + toluene, (v) cyclohexane $+\mathrm{CHCl}_{3}+p$-xylene, (vi) cyclohexane + methylene dichloride $\left(\mathrm{CH}_{2} \mathrm{Cl}_{2}\right)+$ toluene, and (vii) cyclohexane $+\mathrm{CH}_{2} \mathrm{Cl}_{2}+\rho$-xylene, have been measured over a wide concentration range. The results have been fitted to an equation of the type $V^{\mathrm{E}}{ }_{123}=V^{\mathrm{E}}{ }_{12}{ }^{*}$ $+V^{\mathrm{E}}{ }_{23}{ }^{*}+V^{\mathrm{E}} \mathrm{E}_{1{ }^{*}}{ }^{+}+x_{1} x_{2} x_{3} \mid A+B x_{1}\left(x_{2}-x_{3}\right)+C x_{1}{ }^{2}\left(x_{2}\right.$ $\left.-x_{3}\right)^{2} \mid$ where $V^{\mathrm{E}}{ }_{123}$ is the excess volume of mixing per mole of the ternary mixture in which mole fractions of components 1,2 , and 3 are $x_{1}, x_{2}$, and $x_{3}$, respectively. $A, B$, and $C$ are constants which are characteristic of a ternary system and the quantities $V^{\mathrm{E}}{ }_{12}{ }^{*}, V^{\mathrm{E}}{ }_{23}{ }^{*}$, and $V^{\mathrm{E}}{ }_{31}{ }^{*}$ are given by $V^{\mathrm{E}}{ }_{12}{ }^{*}=x_{1} x_{2}\left[A_{12}+B_{12}\left(x_{1}-x_{2}\right)+C_{12}\left(x_{1}\right.\right.$ $\left.\left.-x_{2}\right)^{2}\right], V^{E}{ }_{23}^{*}=x_{2} x_{3}\left[A_{23}+B_{23}\left(x_{2}-x_{3}\right)+C_{23}\left(x_{2}-\right.\right.$ $\left.x_{3}\right)^{2}$, and $V^{\mathrm{E}}{ }_{31}{ }^{*}=x_{1} x_{3}\left(A_{31}+B_{31}\left(x_{1}-x_{3}\right)+C_{31}\left(x_{1}-\right.\right.$ $\left.x_{3}\right)^{2} \mid$, where $A_{12}, B_{12}, C_{12}$, etc. are constants which are determined from the data on excess volumes of mixing for the binaries. The deviations, $\Delta V^{\mathbb{E}}$, of the experimental values of $V^{E}{ }_{123}$ from the appropriate quantities of the three binary systems have been calculated by using the relation $\Delta V^{\mathrm{E}}=V^{\mathrm{E}}{ }_{123}-1 / 2 \mid\left(X_{1}+X_{2}\right) V^{\mathrm{E}}{ }_{12}+\left(X_{2}+X_{3}\right) V^{\mathrm{E}}{ }_{23}+$ $\left.\left(X_{3}+X_{1}\right) V^{E_{31}}\right]$, where $X_{1}, X_{2}$, and $X_{3}$ refer to the number of moles of components 1,2 , and 3 in the ternary system, and the quantities $V^{E}{ }_{12}$ etc. refer to the excess volumes of mixing per mole of a binary mixture in which mole fraction of component 1 is $X_{1} /\left(X_{1}+X_{2}\right)$ and of component 2 is $X_{2} /\left(X_{1}+X_{2}\right)$ etc. The values of $\Delta V^{\mathbb{E}}$ have been found to be positive in the case of all the ternary systems. It is suggested that this is due to weakening of halomethanearomatic interaction by the third component.

Thermodynamic properties of ternary mixtures have been studied by very few workers ( $1,2,5,7$ ). Thermodynamic interpretation of vapor pressure of ternary liquid mixtures was reported by Srivastava and Rastogi (7) several years ago. Quite recently Rastogi, Nath, and Yadava (3) have reported the excess volume of mixing for two ternary systems, viz., (i) quinoline + $\mathrm{CCl}_{4}+$ cyclohexane and (ii) benzene $+\mathrm{CCl}_{4}+$ cyclohexane. The results were fitted to an analytical equation which could not be considered to be a general equation for ternary mixtures. In this paper the results have been fitted by a more general equation and the results are interpreted in terms of ternary interactions and the influence of one component on the binary interaction of the remaining components.

## Experimental Section

(a) Purification of Materials. Benzene (A.R.), toluene (A.R.), and chloroform (A.R.) were subjected to further purification by the method described by Rastogi, Nath, and Misra (4), whereas carbon tetrachloride (A.R.) and methylene dichloride (G.R., S. Merck) were purified by the method described by Vogel ( 9 ). $p$-Xylene (Riedel) was purified by fractional crystallization. The sample thus obtained was subjected to fractional distillation. The
spectroscopically pure sample of cyclohexane (S. Merck) was used without further purification. The densities of the purified components were found to be in good agreement with the values available in literature (8).
(b) Procedure. The excess volumes of mixing were determined by a three-limbed dilatometer shown in Figure 1. Known amounts of the three liquid components were filled over mercury in the limbs $K, L$, and $M$ of the dilatometer with the help of a hypodermic syringe having a bent needle. The stopper $S$ was then tightly inserted in the mouth of the side tube T . The dilatometer (mounted on a wooden stand) was placed in a water thermostat maintained at the required temperature to better than $\pm 0.01^{\circ} \mathrm{C}$. After the contents of the dilatometer had attained the temperature of the thermostat, which was indicated by the constancy of the mercury level in the capillary D , the three liquids were mixed by repeatedly tilting the mixing cell. The volume change on mixing was estimated by noting the change in the height of the mercury level in the capillary before and after mixing by using a cathetometer which could read correct to $\pm 0.001 \mathrm{~cm}$. The measurements of $V^{E}$ for binary mixtures were made with the dilatometer using only two limbs $K$ and $M$. In the present design of the dilatometer, an error in the measurements could be on account of the compressibility of liquid mixtures due to varying pressure of the mercury column in the dilatometer. Calculations showed that the uncertainty due to this factor would be of the order of $1.0 \times 10^{-5} \mathrm{~cm}^{3} \mathrm{~mol}^{-1}$ which can be neglected, since the values of $V^{E}$ are correct to $\pm 0.002 \mathrm{~cm}^{3} \mathrm{~mol}^{-1}$. Also the error on account of dilatation of the vessel would be much less.

The accuracy of the dilatometer was tested using the method of Rastogi, Nath, and Yadava (3). The experimental results of $V^{E}$ for the binary systems benzene $+p$-xylene, cyclohexane +


Figure 1. The dilatometer.

| $x$ | $\begin{gathered} V \in \\ \mathrm{~cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $x$ | $\begin{gathered} V E, \\ \mathrm{~cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $x$ | $\begin{gathered} V \in \\ \mathrm{~cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Benzene $+p$-Xylene |  | $\mathrm{CCl}_{4}+p$-Xylene |  | Cyclohexane $+p$-Xylene |  |
| 0.2479 | 0.140 | 0.0773 | -0.002 | 0.2198 | 0.359 |
| 0.3682 | 0.183 | 0.1132 | -0.005 | 0.2747 | 0.417 |
| 0.3814 | 0.184 | 0.2710 | -0.007 | 0.3383 | 0.494 |
| 0.4741 | 0.201 | 0.3610 | -0.009 | 0.4262 | 0.557 |
| 0.5494 | 0.208 | 0.3908 | -0.007 | 0.4268 | 0.566 |
| 0.5496 | 0.207 | 0.4595 | -0.009 | 0.5230 | 0.619 |
| 0.6091 | 0.201 | 0.4970 | -0.008 | 0.5972 | 0.618 |
| 0.6975 | 0.180 | 0.5336 | -0.008 | 0.7436 | 0.514 |
| 0.8097 | 0.137 | 0.7084 | -0.006 | 0.8049 | 0.455 |
| 0.8584 | 0.109 | 0.8429 | -0.002 | 0.8293 | 0.442 |
|  |  | 0.8554 | -0.005 | 0.8363 | 0.406 |
| Cyclohexane + Toluene |  | Cyclohexane $+\mathrm{CH}_{2} \mathrm{Cl}_{2}$ |  | Cyclohexane $+\mathrm{CHCl}_{3}$ |  |
| 0.2737 | 0.390 | 0.1415 | 0.538 | 0.1313 | 0.235 |
| 0.3668 | 0.479 | 0.2128 | 0.642 | 0.1953 | 0.336 |
| 0.4667 | 0.543 | 0.3209 | 0.820 | 0.2733 | 0.423 |
| 0.5208 | 0.560 | 0.3734 | 0.885 | 0.4032 | 0.522 |
| 0.5226 | 0.567 | 0.4846 | 0.931 | 0.4747 | 0.535 |
| 0.5708 | 0.549 | 05050 | 0.935 | 0.5479 | 0.541 |
| 0.6945 | 0.492 | 0.5350 | 0.937 | 0.6039 | 0.526 |
| 0.8182 | 0.388 | 0.5910 | 0.917 | 0.6683 | 0.490 |
| 0.8529 | 0.312 | 0.6810 | 0.812 | 0.7469 | 0.427 |
|  |  | 0.7868 | 0.623 | 0.8121 | 0.346 |
|  |  | 0.8520 | 0.470 | 0.8401 | 0.309 |
|  |  | 0.8763 | 0.422 | 0.8495 | 0.284 |
|  |  |  |  | 0.8672 | 0.266 |
|  |  |  |  | 0.8774 | 0.254 |
|  |  |  |  | 0.9020 | 0.204 |

Table II. Excess Volumes of Mixing for Ternary Systems at $30^{\circ} \mathrm{C}$

| $x_{2}$ | $x_{3}$ | $\begin{gathered} V_{123} \\ \mathrm{~cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $\begin{gathered} V E_{123}(\mathrm{a}), \\ \mathrm{cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $\begin{gathered} \Delta V^{E} \\ \mathrm{~cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $\begin{gathered} V^{\in}{ }_{123}(\mathrm{~b}) \\ \mathrm{cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $\begin{gathered} \Delta V V^{*} \\ \mathrm{~cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $\begin{gathered} \delta^{a}, \\ \mathrm{~cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{CCl}_{4}(1)+$ Benzene (2) $+p$-Xylene (3) |  |  |  |  |  |  |  |
| 0.1063 | 0.6231 | 0.047 | 0.031 | 0.016 | 0.044 | 0.003 | 0.000 |
| 0.1562 | 0.5862 | 0.071 | 0.044 | 0.027 | 0.066 | 0.005 | 0.000 |
| 0.1802 | 0.5536 | 0.079 | 0.050 | 0.029 | 0.074 | 0.005 | -0.001 |
| 0.2846 | 0.4613 | 0.115 | 0.069 | 0.046 | 0.103 | 0.012 | 0.004 |
| 0.2991 | 0.4487 | 0.114 | 0.071 | 0.043 | 0.106 | 0.008 | 0.000 |
| 0.3694 | 0.3779 | 0.121 | 0.077 | 0.044 | 0.115 | 0.006 | -0.003 |
| 0.4310 | 0.3441 | 0.135 | 0.080 | 0.055 | 0.124 | 0.011 | 0.002 |
| 0.4644 | 0.2976 | 0.126 | 0.078 | 0.048 | 0.119 | 0.007 | -0.002 |
| 0.5464 | 0.2146 | 0.112 | 0.068 | 0.044 | 0.104 | 0.008 | 0.000 |
| 0.6240 | 0.1701 | 0.106 | 0.060 | 0.046 | 0.097 | 0.009 | 0.003 |
| 0.6761 | 0.1508 | 0.096 | 0.056 | 0.040 | 0.093 | 0.003 | -0.002 |
| Cyclohexane (1) $+\mathrm{CCl}_{4}(2)+$ Toluene (3) |  |  |  |  |  |  |  |
| 0.0878 | 0.4110 | 0.497 | 0.274 | 0.223 | 0.486 | 0.011 | 0.000 |
| 0.0895 | 0.1387 | 0.313 | 0.171 | 0.142 | 0.310 | 0.003 | 0.000 |
| 0.0900 | 0.4078 | 0.496 | 0.273 | 0.223 | 0.484 | 0.012 | 0.001 |
| 0.1198 | 0.3197 | 0463 | 0.264 | 0.199 | 0.454 | 0.009 | -0.001 |
| 0.1236 | 0.3200 | 0.460 | 0.263 | 0.197 | 0.452 | 0.008 | -0.002 |
| 0.2369 | 0.4475 | 0.346 | 0.228 | 0.118 | 0.334 | 0.012 | 0.001 |
| 0.2984 | 0.4115 | 0.304 | 0.214 | 0.090 | 0.293 | 0.011 | 0.002 |
| 0.3547 | 0.3721 | 0.271 | 0.203 | 0.068 | 0.263 | 0.008 | 0.001 |
| 0.4517 | 0.1912 | 0.249 | 0.200 | 0.049 | 0.245 | 0.004 | 0.001 |
| 0.5940 | 0.2384 | 0.129 | 0.133 | -0.004 | 0.128 | 0.001 | -0.002 |
| Cyclohexane (1) $+\mathrm{CCl}_{4}(2)+p$-Xylene (3) |  |  |  |  |  |  |  |
| 0.0565 | 0.5567 | 0.512 | 0.275 | 0.237 | 0.504 | 0.008 | 0.000 |
| 0.1070 | 0.1852 | 0.432 | 0.242 | 0.190 | 0.421 | 0.011 | 0.000 |
| 0.1389 | 0.7009 | 0.256 | 0.155 | 0.101 | 0.245 | 0.011 | -0.001 |
| 0.1608 | 0.6092 | 0.340 | 0.206 | 0.134 | 0.323 | 0.017 | 0.000 |
| 0.1753 | 0.1439 | 0.374 | 0.220 | 0.154 | 0.356 | 0.018 | 0.004 |
| 0.2057 | 0.3329 | 0.466 | 0.287 | 0.179 | 0.441 | 0.025 | 0.000 |
| 0.3211 | 0.2467 | 0.382 | 0.262 | 0.120 | 0.357 | 0.025 | -0.004 |
| 0.4674 | 0.3034 | 0.252 | 0.197 | 0.055 | 0.227 | 0.025 | -0.003 |
| 0.5491 | 0.0752 | 0.219 | 0.164 | 0.055 | 0.205 | 0.014 | 0.000 |
| 0.6233 | 0.1519 | 0.190 | 0.166 | 0.024 | 0.170 | 0.020 | 0.001 |


| $x_{2}$ | $x_{3}$ | $\begin{gathered} V_{123}^{E}, \\ \mathrm{~cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $\begin{gathered} V_{123}(\mathrm{a}) \\ \mathrm{cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $\begin{gathered} J V^{E} \\ \mathrm{~cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $\begin{gathered} V_{123}(\mathrm{~b}) \\ \mathrm{cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $\begin{gathered} \Delta V^{E} \\ -\mathrm{cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $\begin{gathered} \delta^{a}, \\ \mathrm{~cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cyclohexane (1) $+\mathrm{CH}_{2} \mathrm{Cl}_{2}(2)+p$-Xylene (3) |  |  |  |  |  |  |  |
| 0.1552 | 0.6191 | 0.450 | 0.388 | 0.062 | 0.502 | -0.052 | -0.001 |
| 0.2127 | 0.5004 | 0.566 | 0.485 | 0.081 | 0.636 | -0.070 | 0.006 |
| 0.2670 | 0.4769 | 0.542 | 0.496 | 0.046 | 0.636 | -0.094 | -0.008 |
| 0.3310 | 0.4307 | 0.557 | 0.513 | 0.044 | 0.654 | -0.097 | -0.002 |
| 0.3596 | 0.3959 | 0.587 | 0.530 | 0.057 | 0.681 | -0.094 | 0.006 |
| 0.4016 | 0.3640 | 0.583 | 0.534 | 0.049 | 0.684 | -0.101 | 0.001 |
| 0.4207 | 0.3247 | 0.621 | 0.557 | 0.064 | 0.729 | -0.108 | -0.001 |
| 0.4566 | 0.2992 | 0.623 | 0.554 | 0.069 | 0.730 | -0.107 | -0.001 |
| 0.5423 | 0.2128 | 0.662 | 0.552 | 0.110 | 0.758 | -0.096 | 0.002 |
| 0.6178 | 0.1577 | 0.656 | 0.517 | 0.139 | 0.736 | -0.080 | -0.001 |
| Cyclohexane (1) $+\mathrm{CHCl}_{3}(2)+$ Toluene (3) |  |  |  |  |  |  |  |
| 0.1610 | 0.6575 | 0.295 | 0.240 | 0.055 | 0.316 | -0.021 | 0.000 |
| 0.2523 | 0.5559 | 0.312 | 0.269 | 0.043 | 0.340 | -0.028 | 0.005 |
| 0.2939 | 0.4461 | 0.382 | 0.335 | 0.047 | 0.433 | -0.051 | -0.006 |
| 0.3468 | 0.4478 | 0.321 | 0.298 | 0.023 | 0.372 | -0.051 | -0.006 |
| 0.3970 | 0.3736 | 0.361 | 0.321 | 0.040 | 0.405 | -0.044 | 0.007 |
| 0.4893 | 0.2627 | 0.376 | 0.330 | 0.046 | 0.425 | -0.049 | 0.003 |
| 0.5231 | 0.2568 | 0.341 | 0.307 | 0.034 | 0.392 | -0.051 | -0.002 |
| 0.5789 | 0.1817 | 0.367 | 0.308 | 0.059 | 0.410 | -0.043 | 0.000 |
| 0.6103 | 0.1548 | 0.363 | 0.297 | 0.066 | 0.402 | -0.039 | 0.001 |
| 0.6487 | 0.0543 | 0.435 | 0.278 | 0.157 | 0.453 | $-0.018$ | 0.000 |
| Cyclohexane (1) $+\mathrm{CHCl}_{3}(2)+p$-Xylene (3) |  |  |  |  |  |  |  |
| 0.1646 | 0.5799 | 0.437 | 0.333 | 0.104 | 0.466 | -0.029 | 0.002 |
| 0.1695 | 0.6366 | 0.359 | 0.286 | 0.073 | 0.390 | -0.031 | -0.004 |
| 0.2495 | 0.5591 | 0.380 | 0.313 | 0.067 | 0.411 | -0.031 | 0.004 |
| 0.3297 | 0.4776 | 0.387 | 0.332 | 0.055 | 0.430 | -0.043 | -0.003 |
| 0.4605 | 0.3714 | 0.371 | 0.317 | 0.054 | 0.407 | -0.036 | 0.000 |
| 0.6154 | 0.2054 | 0.374 | 0.304 | 0.070 | 0.399 | -0.025 | 0.000 |
| 0.7199 | 0.0669 | 0.377 | 0.263 | 0.114 | 0.387 | -0.010 | -0.001 |
| 0.7479 | 0.0779 | 0.334 | 0.241 | 0.093 | 0.342 | -0.008 | 0.002 |
| Cyclohexane (1) $+\mathrm{CH}_{2} \mathrm{Cl}_{2}(2)+$ Toluene (3) |  |  |  |  |  |  |  |
| 0.1358 | 0.6511 | 0.386 | 0.333 | 0.053 | 0.423 | -0.037 | -0.008 |
| 0.1996 | 0.5823 | 0.422 | 0.385 | 0.037 | 0.478 | -0.056 | -0.006 |
| 0.2924 | 0.4910 | 0.461 | 0.437 | 0.024 | 0.540 | -0.079 | 0.001 |
| 0.3597 | 0.4185 | 0.499 | 0.471 | 0.028 | 0.590 | -0.091 | 0.006 |
| 0.3833 | 0.3930 | 0.507 | 0.480 | 0.027 | 0.607 | -0.100 | 0.003 |
| 0.4743 | 0.3087 | 0.541 | 0.492 | 0.049 | 0.641 | -0.100 | 0.009 |
| 0.5316 | 0.2432 | 0.574 | 0.501 | 0.073 | 0.677 | -0.103 | 0.004 |
| 0.6124 | 0.1643 | 0.596 | 0.485 | 0.111 | 0.694 | -0.098 | -0.011 |
| 0.6872 | 0.0909 | 0.634 | 0.448 | 0.186 | 0.701 | -0.067 | -0.011 |

${ }^{a} \delta$ is the deviation in the experimental value of $V^{E}{ }_{123}$ from that calculated according to eq 2.
toluene, $\mathrm{CCl}_{4}+p$-xylene, cyclohexane $+\mathrm{CH}_{2} \mathrm{Cl}_{2}$, cyclohexane $+p$-xylene, and cyclohexane $+\mathrm{CHCl}_{3}$ are recorded in Table I, and have been fitted by the method of least squares to the equations given in Table III. The experimental values of the excess volume of mixing for the various ternary systems are recorded in the third column of Table II.

## Results and Discussion

The excess volumes of mixing, $V^{E}{ }_{123}$, for a ternary mixture containing $X_{1}, X_{2}$, and $X_{3}$ moles of components 1,2 , and 3 , respectively, may be expressed as

$$
\begin{align*}
V^{E} & =\frac{1}{2}\left[\left(X_{1}+X_{2}\right) V^{E_{12}}+\left(X_{2}+X_{3}\right) V^{E_{23}}\right. \\
& \left.+\left(X_{3}+X_{1}\right) \vee^{E_{31}}\right] \tag{1}
\end{align*}
$$

where $V^{E}{ }_{12}$ is the excess volume of mixing per mole of a binary mixture in which mole fraction of component 1 is $X_{1} /\left(X_{1}+X_{2}\right)$ and of component 2 is $X_{2} /\left(X_{1}+X_{2}\right), V^{E}{ }_{23}$ is the excess volume of mixing per mole of a binary mixture in which mole fraction of component 2 is $X_{2} /\left(X_{2}+X_{3}\right)$ and of component 3 is $X_{3} /\left(X_{2}+\right.$ $X_{3}$ ), and $V^{E_{31}}$ is the excess volume of mixing per mole of a binary mixture in which mole fraction of component 3 is $X_{3} /\left(X_{3}+X_{1}\right)$ and of component 1 is $X_{1} /\left(X_{3}+X_{1}\right)$. The values of $V{ }^{3} 123$ ob-
tained from eq 1 by making use of the equations of the excess volumes of mixing for the various binary systems (see Table III) have been represented as $V^{E}{ }_{123}(a)$ in fourth column of Table II. The deviations $\Delta V^{E}=V^{E}{ }_{123}-V^{E}{ }_{123}($ a $)$, in the experimental values of the excess volumes of mixing for the ternary systems from those of $V^{E}{ }_{123}(a)$, are given in the fifth column of Table II.

The experimental results of $V^{E}{ }_{123}$ for the various ternary systems have been fitted by the method of least squares to the equation

$$
\left.\begin{array}{rl}
V_{123}=V^{E} & V_{2}^{*}+E_{23}{ }^{*}
\end{array}\right)
$$

where $x_{1}, x_{2}$, and $x_{3}$ are the mole fractions of components 1 , 2 , and 3 , respectively, in the ternary mixture and $A, B$, and $C$ are constants for a ternary system. The quantities $V^{E}{ }_{12}{ }^{*}, V^{E}{ }_{23}{ }^{*}$, and $V_{31}{ }^{*}$ are given by

$$
\begin{align*}
& V^{E}{ }_{12}^{*}=x_{1} x_{2}\left[A_{12}+B_{12}\left(x_{1}-x_{2}\right)+C_{12}\left(x_{1}-x_{2}\right)^{2}\right]  \tag{3}\\
& V^{E_{23}}=x_{2} x_{3}\left[A_{23}+B_{23}\left(x_{2}-x_{3}\right)+C_{23}\left(x_{2}-x_{3}\right)^{2}\right]  \tag{4}\\
& V^{E_{31}}{ }^{*}=x_{1} x_{3}\left[A_{31}+B_{31}\left(x_{1}-x_{3}\right)+C_{31}\left(x_{1}-x_{3}\right)^{2}\right] \tag{5}
\end{align*}
$$

where $A_{12}, B_{12}, C_{12}$, etc. are constants which are determined

| System | Equation fitting the data ${ }^{g}: V^{E}\left(\mathrm{~cm}^{3} \mathrm{~mol}^{-1}\right)$ |
| :---: | :---: |
| Benzene + p-xylene ${ }^{\text {a }}$ | $\mathrm{x}_{2} x_{3}\left[0.8187+0.1226\left(x_{2}-x_{3}\right)-0.0379\left(x_{2}-x_{3}\right)^{2}\right]$ |
| Cyclohexane + toluene ${ }^{\text {a }}$ | $x_{1} x_{3}\left[2.2044+0.4999\left(x_{1}-x_{3}\right)-0.0322\left(x_{1}-x_{3}\right)^{2}\right]$ |
| Cyclohexane $+p$-xylene ${ }^{\text {a }}$ | $x_{1} x_{3}\left[2.3983+0.7161\left(x_{1}-x_{3}\right)+0.2693\left(x_{1}-x_{3}\right)^{2}\right]$ |
| $\mathrm{CCl}_{4}+p$-xylene ${ }^{\text {a }}$ | $x_{1} x_{3}\left[-0.03224+0.0064\left(x_{1}-x_{3}\right)-0.00325\left(x_{1}-x_{3}\right)^{2}\right]$ |
| Cyclohexane $+\mathrm{CHCl}_{3}{ }^{\text {a }}$ | $\mathrm{x}_{1} \mathrm{x}_{2}\left[2.1704+0.1377\left(x_{1}-x_{2}\right)+0.05035\left(x_{1}-x_{2}\right)^{2}\right]$ |
| Cyclohexane $+\mathrm{CH}_{2} \mathrm{Cl}_{2}{ }^{\text {a }}$ | $\mathrm{x}_{1} x_{2}\left[3.7153-0.2605\left(x_{1}-x_{2}\right)+0.5771\left(x_{1}-x_{2}\right)^{2}\right]$ |
| $\mathrm{CCl}_{4}+$ benzene $^{\text {b }}$ | $0.043 x_{1} x_{2}$ |
| Cyclohexane $+\mathrm{CCl}_{4}{ }^{\text {c }}$ | $0.638 x_{1} x_{2}$ |
| $\mathrm{CCl}_{4}+$ toluene ${ }^{\text {d }}$ | $x_{2} x_{3}\left[-0.1524-0.0204\left(x_{2}-x_{3}\right)+0.0243\left(x_{2}-x_{3}\right)^{2}\right]$ |
| $\mathrm{CHCl}_{3}+$ toluene ${ }^{e}$ | $x_{2} x_{3}\left[0.180-0.016\left(x_{2}-x_{3}\right)-0.040\left(x_{2}-x_{3}\right)^{2}\right]$ |
| $\mathrm{CHCl}_{3}+p$-xylene ${ }^{e}$ | $x_{2} x_{3}\left[0.585+0.085\left(x_{2}-x_{3}\right)-0.165\left(x_{2}-x_{3}\right)^{2}\right]$ |
| $\mathrm{CH}_{2} \mathrm{Cl}_{2}+$ toluene ${ }^{t}$ | $x_{2} x_{3}\left[0.653+0.320\left(x_{2}-x_{3}\right)-0.048\left(x_{2}-x_{3}\right)^{2}\right]$ |
| $\mathrm{CH}_{2} \mathrm{Cl}_{2}+p$-xylene ${ }^{f}$ | $x_{2} x_{3}\left[0.922+0.398\left(x_{2}-x_{3}\right)+0.020\left(x_{2}-x_{3}\right)^{2}\right]$ |
| a Equations based on the R. P., Nath, J., Misra, J., J. to the mole fractions of cyc $\mathrm{CCl}_{4}+p$-xylene, and benz | ${ }^{\mathrm{b}}$ Rastogi, R. P., Nath, J., Indian J. Chem., 5, 249 (1967). ${ }^{\text {c }}$ See ref 3. ${ }^{\sigma}$ Rastogi, ${ }^{t}$ Nigam, R. K., Mahl, B. S., Indian J. Chem., 9, 1250 (1971). ${ }^{g} x_{1}, x_{2}$, and $x_{3}$ refer respectively, in the various binary systems except in the case of $\mathrm{CCl}_{4}+$ benzene, e mole fractions of $\mathrm{CCl}_{4}$, benzene, and $p$-xylene, respectively. |

Table IV. Values of the Constants A, B, C, and $\sigma$ al $30^{\circ} \mathrm{C}$

| System | $\begin{gathered} A, \\ \mathrm{~cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $\begin{gathered} B \\ \mathrm{~cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $\begin{gathered} C \\ \mathrm{~cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ | $\begin{gathered} \sigma \\ \mathrm{cm}^{3} \mathrm{~mol}^{-1} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{CCl}_{4}+$ benzene $+p$-xylene | 0.2652 | 0.3432 | -1.9167 | 0.002 |
| Cyclohexane $+\mathrm{CCl}_{4}+$ toluene | 0.196 | -1.621 | 6.026 | 0.002 |
| Cyclohexane $+\mathrm{CCl}_{4}+$ p-xylene | 0.832 | 0.688 | -1.363 | 0.002 |
| Cyclohexane $+\mathrm{CHCl}_{3}+$ toluene | -1.479 | -3.399 | 10.282 | 0.005 |
| Cyclohexane $+\mathrm{CHCl}_{3}+$ p-xylene | -1.284 | 1.386 | 13.045 | 0.003 |
| Cyclohexane $+\mathrm{CH}_{2} \mathrm{Cl}_{2}+$ toluene | -3.078 | 10.829 | 28.721 | 0.009 |
| Cyclohexane $+\mathrm{CH}_{2} \mathrm{Cl}_{2}+$ p-xylene | -2.931 | -5.987 | -6.288 | 0.005 |

from the data on excess volume of mixing for the binaries. The quantities $V^{E_{12}}{ }^{*}, V^{E_{23}}$, and $V^{E_{31}}$. can be estimated by making use of the equations (see Table III) for the excess volumes of mixing for the three binaries. As for example, the quantities $V^{E}{ }_{12}{ }^{*}, V^{E_{23}}$, and $V^{E_{31}}{ }^{*}$, in the case of the ternary system cyclohexane $+\mathrm{CHCl}_{3}+$ toluene, as ascertained from the equations (see Table III) for the excess volumes of mixing for the three binary systems cyclohexane $+\mathrm{CHCl}_{3}, \mathrm{CHCl}_{3}+$ toluene and cyclohexane + toluene, are represented as

$$
\begin{align*}
& V E_{12}=x_{1} x_{2}\left[2.1704+0.1377\left(x_{1}\right.\right. \\
& \left.\left.\quad-x_{2}\right)+0.05035\left(x_{1}-x_{2}\right)^{2}\right]  \tag{6}\\
& V E_{23}=x_{2} x_{3}\left[0.180-0.016\left(x_{2}\right.\right. \\
& \left.\left.\quad-x_{3}\right)-0.040\left(x_{2}-x_{3}\right)^{2}\right]  \tag{7}\\
& V E_{31^{*}=}=x_{1} x_{3}\left[2.2044+0.4999\left(x_{1}\right.\right. \\
& \left.\left.\quad-x_{3}\right)-0.0322\left(x_{1}-x_{3}\right)^{2}\right] \tag{8}
\end{align*}
$$

The mole fractions $x_{1}, x_{2}$, and $x_{3}$ of components 1,2 , and 3 ,
 eq 3-5 or eq 6-8 have been kept the same (see Table II) as those
 for the various ternary systems are represented as $V^{E}{ }_{123}$ (b) in the sixth column of Table II. Accordingly the deviations, $\Delta V^{E *}$ $=V^{E}{ }_{123}-\left(V^{E}{ }_{12}{ }^{*}+V^{E_{23}{ }^{*}}+V^{E_{31}}{ }^{*}\right)$, of the experimental values of $V^{E}{ }_{123}$ from those of the sum, $V^{E}{ }_{12^{*}}+V^{E_{23}}{ }^{*}+V^{E}{ }_{31^{*}}$, are given in the seventh column of Table II. The values of the constants $A, B$, and $C$ along with the standard deviations, $\sigma$, in the experimental values of $V^{E}{ }_{123}$ from those obtained from eq 2 are given in Table IV. Table II shows that eq 2 fits the experimental
values of $V^{E}{ }_{123}$ accurately in the case of the various ternary systems.

The ternary data on the eight systems studied by us show that $\Delta V^{E}$ is positive for (i) benzene $+\mathrm{CCl}_{4}+$ cyclohexane (3), (ii) $\mathrm{CCl}_{4}+$ benzene $+p$-xylene, (iii) cyclohexane $+\mathrm{CCl}_{4}+$ toluene and (iv) cyclohexane $+\mathrm{CCl}_{4}+p$-xylene, ( $v$ ) cyclohexane + $\mathrm{CHCl}_{3}+$ toluene, (vi) cyclohexane $+\mathrm{CHCl}_{3}+p$-xylene, (vii) cyclohexane $+\mathrm{CH}_{2} \mathrm{Cl}_{2}+$ toluene, and (viii) cyclohexane + $\mathrm{CH}_{2} \mathrm{Cl}_{2}+p$-xylene. This can be explained to be due to the weakening of donor-acceptor interaction between halomethanes and aromatics by cyclohexane, since the molecular charge distribution is bound to be affected by the surrounding molecules as is experimentally found to be true in many cases (6).

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